## Mathematics test

## Paper 2 Calculator allowed

Please read this page, but do not open your booklet until your teacher tells you to start. Write your name and the name of your school in the spaces below.

## First name

$\qquad$
Last name $\qquad$
School

## Remember

- The test is 1 hour long.
- You may use a calculator for any question in this test.
- You will need: pen, pencil, rubber, ruler, a pair of compasses and a scientific or graphic calculator.
- $\quad$ Some formulae you might need are on page 2.
- This test starts with easier questions.
- Try to answer all the questions.
- Write all your answers and working on the test paper do not use any rough paper. Marks may be awarded for working.
- Check your work carefully.
- Ask your teacher if you are not sure what to do.

|  | For marker's <br> use only | Total marks |
| :--- | :--- | :--- |
|  | Borderline check |  |
|  |  |  |

## Instructions

## Answers

This means write down your answer or show your working and write down your answer.

## Calculators

You may use a calculator to answer any question in this test.


1. Look at the diagram, made from four straight lines.

The lines marked with arrows are parallel.


Work out the sizes of the angles marked with letters.
$\qquad$ $\circ$
$b=$ $\qquad$ 0
$c=$ $\qquad$ $\circ$

$$
d=
$$

$\qquad$ $\circ$
2. Look at this equation.

$$
3 a+20=4 a+k
$$

(a) If $\boldsymbol{a}=15$, find the value of $k$

$$
k=
$$

$\qquad$
1 mark
(b) If $\boldsymbol{a}=-15$, find the value of $k$

$$
k=
$$

3. Each shape below is made from five cubes that are joined together.

Complete the missing diagrams below.

4. Look at these pairs of number sequences.

The second sequence is formed from the first sequence by adding a number or multiplying by a number.

Work out the missing $n$th terms.
(a)

$$
5, \quad 9, \quad 13, \quad 17, \quad \ldots
$$

$n$th term is

$$
4 n+1
$$

$6,10,14,18, \ldots$ $n$th term is $\qquad$
(b)

$$
12, \quad 18, \quad 24, \quad 30, \quad \ldots
$$

$n$th term is

$$
6 n+6
$$

$6, \quad 9,12,15$, $n$th term is $\qquad$
(c) $\square$ $n$th term is

$$
5 n-3
$$

$4,14,24,34$,
... $n$th term is $\qquad$
5. Look at the square grids.

Each diagram shows an enlargement of scale factor 2
The centre of this enlargement is marked with a cross.


Where is the centre of enlargement in these diagrams?
Mark each one with a cross.


6. Kate asked people if they read a daily newspaper.

Then she wrote this table to show her results.

| No | 80 people $=40 \%$ |
| :---: | :---: |
| Yes | 126 people $=60 \%$ |

The values in the table cannot all be correct.
(a) The error could be in the number of people.

Complete each table to show what the correct numbers could be.


| No | people $=40 \%$ |
| :---: | :---: |
| Yes | 126 people $=60 \%$ |

(b) The error could be in the percentages. Complete the table with the correct percentages. 1

| No | 80 people $=\ldots \%$ |
| :---: | :---: |
| Yes | 126 people $=\square$ |

7. The graph shows information about the diameters and heights of a sample of three types of tomato.

The dotted lines on the graph can be used to decide which type of tomato each point is likely to represent.


(a) The diameter of a tomato of type $\mathbf{C}$ is $\mathbf{1 1} \mathbf{~ c m}$.

What would you expect its height to be?
(b) The diameter of a different tomato is 3.2 cm . Its height is 5.8 cm . Which of the three types of tomato is it most likely to be?
$\square$ A $\square$ B $\square$ C

Explain your answer.
(c) Which type of tomato is most nearly spherical in shape?
$\geqslant$ $\square$ B $\square$ C
$\geqslant$
$\square$
A
Explain your answer.
(d) You can find the approximate volume of a tomato by using this formula:

$$
\mathrm{V}=\frac{1}{6} \pi d^{2} h \quad \begin{aligned}
& \mathrm{V} \text { is the volume, } \\
& d \text { is the diameter, } \\
& h \text { is the height. }
\end{aligned}
$$

The diameter and the height of a tomato are both $\mathbf{3 . 5 \mathrm { cm }}$.
What is the approximate volume of this tomato?

$$
\mathrm{cm}^{3}
$$

$\square$
8. Multiply out these expressions.

Write your answers as simply as possible.

$$
5(x+2)+3(7+x)
$$

$$
(x+2)(x+5)
$$

9. In a wildlife park in Africa, wardens want to know the position of an elephant in a certain area.

They place one microphone at each corner of a $\mathbf{4 k m}$ by $\mathbf{4 k m}$ square.
Each microphone has a range of $3 \frac{1}{2} \mathrm{~km}$.

The elephant is out of range of microphones $\mathbf{A}$ and $\mathbf{B}$.

Where in the square could the elephant be?
Show the region accurately on the diagram, and label the region $\mathbf{R}$.


## Scale

2 cm to 1 km
10. Here are the rules for an algebra grid.


Use these rules to complete the algebra grids below.
Write your expressions as simply as possible.

11. This shape is made of four congruent kites meeting at a point.


Calculate the size of angle $k$
$k=$ $\qquad$
2 marks
12. Look at the diagram of a cuboid.


The volume of the cuboid is $100 \mathrm{~cm}^{3}$

What could the values of $x$ and $y$ be?
Give two possible pairs of values.
$\qquad$ $y=$ $\qquad$

$$
x=
$$ $y=$ $\qquad$

1 mark
13. A pupil wants to investigate a report that Belgian one euro coins are biased in favour of heads.

Here is her plan for the investigation.

I will spin 20 Belgian one euro coins to give one set of results.
I will do this $\mathbf{1 0}$ times to give a total of $\mathbf{2 0 0}$ results to work out an estimated probability of spinning a head.

If this probability is greater than $56 \%$ my conclusion will be that Belgian one euro coins are biased in favour of heads.

The table shows the 10 sets of results.

| Number of each set of $\mathbf{2 0}$ coins that showed heads |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 13 | 11 | 11 | 12 | 12 | 11 | 9 | 10 | 11 |

Using the pupil's plan, what should her conclusion be?
You must show your working.
14. The diagram shows a shaded rectangle.

It is divided into four smaller rectangles, labelled $A, B, C$ and $D$.


Not drawn accurately

The ratio of area $\mathbf{C}$ to area $\mathbf{B}$ is $\mathbf{1 : 2}$
Calculate area A.
$\qquad$
$\mathrm{cm}^{2}$
15. Field voles are small animals that do not live for very long.

A scientist recorded data on 1000 of these voles that were born on the same day.
The graph shows how many voles were still alive after a number of weeks.

Number of voles still alive


Use the graph to answer these questions.
(a) Estimate the probability that a field vole will live to be at least 20 weeks old.

$\qquad$
1 mark
(b) A field vole is 40 weeks old.

Estimate the probability that it will live to be at least 50 weeks old.
$\qquad$
1 mark
16. Films at the cinema and films on television are shown at different speeds.


At the cinema a film lasts 175 minutes.
How many minutes does the same film last on television?
minutes
17. The graph shows the straight line with equation $\boldsymbol{y}=\boldsymbol{x}+\mathbf{1}$

This straight line passes
through the point $(\mathbf{0}, \mathbf{1})$

(a) Write the equations of two different straight lines that also pass through the point $(0,1)$
$\qquad$ and $\qquad$
(b) The straight line with equation $x+y=5$ is perpendicular to $y=x+1$


Write the equation of a different straight line that is also perpendicular to $y=x+1$
18. A housing report gave this information.

In the year 2001, the population of England was 49.87 million people.
Most of these people lived in households.
The total number of households was $\mathbf{2 0 . 9 7}$ million.
The average (mean) household size was 2.34 people.

In the year 2001, what percentage of people in England did not live in households?

Give your answer to 1 decimal place.
19. Six cubes each have a surface area of $24 \mathrm{~cm}^{2}$

They are joined together to make a cuboid.

What could the surface area of this cuboid be?
There are two different answers. Write them both.




$\qquad$ c
$\mathrm{cm}^{2}$ o $\qquad$ $\mathrm{cm}^{2}$
20. The diagram shows five points joined with four straight lines.
$B C$ and $A D$ are parallel.
$B C E$ and $A D E$ are isosceles triangles.


Not drawn
D
accurately

The total length of the four straight lines is 40 cm .
What is the length of EA?
$\qquad$
21. I have three fair dice, each numbered 1 to 6


I am going to throw all three dice.
What is the probability that all three dice will show the same number?
22. Since 1952 the total number of people living in Wales has increased by about one eighth.

The total number of people living in Wales now is about 3 million.

About how many people lived in Wales in 1952?
$\qquad$ million
23. Engineers have worked on the leaning tower of Pisa to make it safe.


A website gave this information about the tower before the work.


Give calculations to show that the information cannot all be true.

## END OF TEST

